**Chapter 1: Measurement**

Measurement is widely used in business and industry, in science and technology, in manufacturing and engineering, as well as in many aspects of daily living.

Measurement gives a number to a particular characteristic of a person, an object or a concept. When measurements are made, they are expressed quantitatively as numbers. This, therefore, entails the study of the standard u8nits of measure and the proficient use of measuring devices.

Ancient people made use of counting to measure objects and distances. Now, modern technology makes possible the use of measuring devices such as counters, scales, meters, transits, spectroscopes, and the like.

**1.1: The History of Measurement**

The idea of measurement dates back to the ancient civilizations of Egypt, Babylonia and China. Through trade and conquest, systems of measurements spread to other parts of the world.

**The Ancient System**

The ancient system of measurement makes use of body parts.  
The basic units used by the early Egyptians are:

*Cubit:* the length of the distance from the elbow to the extend fingertip  
*Digit:* the subdivisions of the cubit, supposed to be a finger’s breadth  
*Small span/large span:* the length of the distance covered with the palms of the hand.

The basic unit used by the early Babylonians is:

*Mina: the earliest known unit of weight.*

The basic units used by the early Greeks are:

*Finger:* the basic unit of length  
*Olympic cubit:* the equivalent of twenty four fingers  
*Talent:* the basic unit of weight  
*Metrites:* the basic unit of liquid measure

The Chinese system of measurement employed parts of the body, such as the distance from the pulse to the base of the thumb.

*Shih/Tan:* the basic units of weight  
*Chih/Chang:*  the basic units of length

The standard measure for grain included its *weight* and its *pitch* when struck. This gives the reason why the inclusion of the acoustic dimension is its unique characteristic. Another characteristic of the Chinese measure is the use of the *decimal notation.*

**The Medieval System**

The medieval system of measurement was an offshoot of the Roman system which was a mixture of the Babylonian, the Egyptian and the Chinese systems.

*Libra:* the medieval unit of weight  
*Roman mile:* the unit of measure for distance with varying number of feet and yards.  
*pinte:* the basic unit of liquid measure  
*quart:* the unit of dry measure similar to the modern English quart.

**The English System**

The English system used by Great Britain and its colonies:  
 *inch:* length of 3 barley corns  
 *foot:* length equivalent to 12 inches  
 *yard:* the standard unit of length divided into 3 feet  
 *perch:*  equivalent to 5.5 yards  
 *acre:* 4 rods wide by 40 rods long  
 *furlong:*  standardized as one-eighth of a mile  
 *English Pound:*  a troy weight  
 *avoirdupois:*  used for goods that had to be weighed  
 stone: a multiple of the English pound

**The Metric System**

The metric system came about as a result of the French Revolution. By 1799, a new law in France defined the standard units of measure.

*Meter:* for length  
 *gram:* for weight  
 *liter:* for liquid volume  
 *are:* for area  
 *stere:*  for volume

**The International System**

The *Systeme International d’ Unites* (SI) was extablished in October 1960 by the 11th General Conference on Weights and Measures in Paris.  
 *meter:  
 kilogram:  
 second:  
 ampere:*

**1.2: Measures and Measuring Devices**

The results of measuring are merely near approximations since measurements a re not always exact. There is often a relative error involved.  
 Accuracy of measurements depends on two factors:  
 1. The skill of the person doing the measuring; and  
 2. The precision of the instrument used in measuring.  
 The first factor can easily be developed through constant practice while the second factor is totally dependent upon the measuring device.  
 As noted from the development of measurements as well as observed from daily life activities, different quantities require different units of measure and different measuring devices.  
 Originally, our forefathers made use of their body parts to measure lengths and distances. Unfortunately, these nonstandard units proved inconvenient, paving the way for standardized units like the metric system or *Systeme International d’ Unites* (SI). This system of measurement is the one commonly used by most countries today.

**1.2.1: Measure of Length**

The fundamental unit of length in the metric system is the *meter*. It is a decimal system for measurement where multiples and fractions of the basic unit(meter) correspond to powers of ten.

**TEST YOURSELF  
 Choose the most realistic unit of measure for each.**

1. Length of a ballpen
2. Width of a blackboard
3. Thickness of a notebook
4. Length of a pair of pants
5. Height of a tree
6. Height of a 12 year old boy
7. Length of a curtain material
8. Width of a street
9. Diameter of a 5c coin
10. Thickness of a glass

**Convert the following. (Use the metric converter.)**

1. 2km to m = **2000 m**
2. 354 cm to m = **3.54 m**
3. 7.15 m to cm = **715 cm**
4. 275 dm to m = **27.5 m**
5. 80 mm to m = **0.08 m**
6. 2650 m to km = **2.65 km**
7. 0.09 m to mm = **90 mm**
8. 8.75 m to km = **0.00875 km**
9. 60.8 km to m = **60,800 m**
10. 4585 cm to m = **45.85 m**

**PROBLEMS**

1. **A boy ran a distance of 5.8 kilometers . How many meters did he run?**
   1. **5.8 x 1000 = 5,800 meters**
2. **A car traveled a distance of 23.6 kilometers. How many meters did the car travel?**
   1. **23.6 x 1000 = 23,600 meters**
3. **A piece of wood is 470 centimeters long. How long is it in meters?**
   1. **470 x 0.01 = 4.7 meters**
4. **Loida walked 204 meters to her classmate’s house and together they walked 523 meters to school. How many kilometers was covered by Loida alone?**
   1. **204 x 0.001 = 0.204 kilometers**
5. **Ben traveled a distance of 126 kilometers in 2 ½ hours. How many meters did Ben travel? How many minutes did it take him to travel 126 kilometers?**
   1. **126 x 1000 = 126,000 meters.**
   2. **(2 x 60) + (60/2) = 120 + 30 = 150 minutes.**
6. **Jose walks 378 meters while Rene walks 0.67 kilometer. What is the difference between the distances they walked in centimeters?**
   1. **((0.67 x 1000) - 378) x 100 = (670 - 378) x 100 = 29,200 centimeters**
7. **A book is 48 millimeters thick. How thick is the book in centimeters?**
   1. **48 x 0.1 = 4.8 centimeters.**
8. **Luisa needs 2.3 meters of cloth for her project. How many decimeters of cloth does she need?**
   1. **2.3 x 10 = 23 decimeters.**

**1.2.2: Measure of Area**

The metric system uses the *square meter* (m2) as the unit of area. A square meter is a square 1 meter long on each side.

A *square centimeter*, which is a square 1 cm long on each side, is used to measure smaller areas like a piece of pad paper, a photograph, or the surface of a desk.

A *square millimeter,* which is a square 1 mm long on each side, is used to measure microscopic objects like those on a microscope side.

The area of a square 10 m on each side is called an *are* which is used to measure garden plots or building lots. An area equivalent to 100 ares is called a *hectare* which is used to measure big farms and ranches. Very large-areas, like areas of cities and states, are reported in *square kilometers.*

**TEST YOURSELF**

**Answer the following.**

1. **How many square meters are in one square kilometer?**
2. **A square meter is equivalent to how many square millimeters?**
3. **What is common name for dam2? hm2?**
4. **How many decimal places to the right do we move to change km2 to m2?**
5. **How many square meters are in one hectare?**

**Choose the most realistic unit of measure of area for each.**

1. **The area of the front cover of a book**
2. **The total area of a big estate/farm**
3. **The floor area of a small house**
4. **The surface area of a microchip**
5. **The surface area of a blackboard**

**Convert the following. (Use the metric converter.)**

1. **0.05cm2 to mm2**
2. **1.87m2 to cm2**
3. **610 dam2 to km2**
4. **0.398 km2 to m2**
5. **7510 mm2 to m2**
6. **1124 mm2 to cm2**
7. **0.0014 km2 to ha**
8. **9625 m2 to ha**
9. **215 a to ha**
10. **7.4 ha to m2**

**PROBLEMS**

**Solve the problems**

1. **A man is buying a lot while measures 8760 square meters. How many hectares of land is he buying?**
2. **Mrs. Reyes is selling a piece of land which measures 3.81 hectares. If the selling price is P2,500 per square meter, how much will she receive from the sale of her land?**
3. **If 3748 areas of land is divided into four equal parts, how many square meters will each part be?**
4. **A piece of cardboard measures 64 cm by 48 cm. What is its area in square meters?**
5. **If the area of a rectangular garden lot is 144 m2, how many square decimeters of grass are needed to fill it?**
6. **How many square meters of wall paper are needed to cover the walls of a room 12 m by 4 m?**

**1.2.3 Measure of Volume and Capacity**

The metric system uses the liter (L) as the fundamental unit of volume. It represents the volume of a cube that measures 10 cm or 1 dm on each edge.

Very small volumes are measured in milliliters, like liquid medicine in milliliter bottles. Large are measured in cubic meters (m3), like water in tanks, reservoirs or swimming pools.

A liter cube can be filled with a 10 x 10 array of centimeter cubes to cover its bottom, and 10 layers of this array can fill the liter cube to the top. Thus, 1 liter or 1 cubic decimeter is equivalent to 1000 cm3.

**TEST YOURSELF**

**Choose the most realistic unit of measure of volume/capacity.**

1. **A bucket of water**
2. **A can of soda**
3. **A tablespoon of sugar**
4. **A cup of coffee**
5. **A glass of juice**
6. **A can of gasoline**

**Convert the following. (Use the metric converter.)**

1. **120 cm3 to m3**
2. **77 m3 to cm3**
3. **622 cm3 to m3**
4. **3.7 m3 to L**
5. **0.003 m3 to cm3**
6. **2.3 L to m3**
7. **0.15 km3 to m3**
8. **830 m3 to km3**
9. **578 cm3 to m3**
10. **6.4 m3 to L**

**PROBLEMS**

**Solve the problems.**

1. **A boy fills a drum with 375 cubic decimeters of water. How many cubic meters of water is in the drum?**
2. **A basin contains 670 cubic millimeters of water. How many liters of water is in the basin?**
3. **A tank contains 15.6 liters of gasoline. How many cubic meters of gasoline is in the tank?**
4. **Which is the most realistic measure of volume for a bottle of soda: 473 mL, 473 cL, or 473 L?**
5. **A tablespoon of syrup is about 15 mL. What part of a liter can a tablespoon hold?**

**1.2.4 Measure of Mass**

The mass of an object is the amount of matter it contains. The basic unit of mass in the metric system is the *kilogram*(kg). A kilogram is the weight of 1 liter of water in its densest state. A milliliter of water weighs 1/1000 of a kilogram, which is called a *gram* (g).

Thus, 1000 grams is equivalent to 1 kilogram. Grams is used for small weights such as ingredients in recipes or nutritional contents of various foods. Remember also the meaning of the prefixes in connection with the measures of mass, such as milligram, centigram, decigram, dekagram, hectogram, and kilogram.

A *platform* balance is an instrument used in measuring the mass of small objects. It is usually accurate to the nearest 0.01 gram. Before using the platform balance, it is important to make sure that the instrument is clean and dry, with the pointer at its position of rest. The object to be weighed is placed on one pan and the standard mass on the other. Keep on adding or removing the standard mass until the 2 pans are balanced and the pointer is at its position of rest.

A weighing scale for commercial use is more convenient and easier to manipulate, but not as accurate. The object to be weighed is placed on a pan and the pointer of the instrument moves through the unit divisions to the point which indicates the weight of the object.

**TEST YOURSELF**

**Choose the most realistic unit of mass for each of the following.**

1. **A pencil**
2. **A baby**
3. **A pail of water**
4. **A teaspoon of salt**
5. **A glass of milk**
6. **A tablespoon of flour**
7. **A basketball**
8. **A car**
9. **A piece of pad paper**
10. **A paper clip**

**Convert the following measure of mass.**

1. **8 kg to g**
2. **2.5 kg to g**
3. **850 mg to g**
4. **370 cg to mg**
5. **75 dg to mg**
6. **3000 g to kg**

**PROBLEMS**

**Solve the problems.**

1. **The mass of one sachet of coffee is 0.005 kilograms. What is its equivalent net weight in grams?**
2. **The content of one bag of powdered juice is 750 grams. How many kilograms are in the bag?**
3. **A girl carries her schoolbag weighing 2.48 kilograms. How much weight in grams is she carrying?**
4. **A bridge can support a mass of 2.8 tonnes. How many kilograms can the bridge support?**
5. **A boy weighing 27.6 kilograms sits on one end of a seesaw. How many grams should another boy weigh if he is to balance the first boy on the opposite end?**
6. **The mass of a box of soap is 460 grams. What is the mass of the box of soap in kilograms? In milligrams?**